Aeroelastic tailoring Comp-Eco workshop

**Roeland De Breuker** 



#### This is a team effort in Delft ...

- Staff members:
  - Jurij Sodja
  - Sherry Wang
  - Daniël Peeters
  - Christos Kassapoglou
- (PhD) Researchers:
  - Terence Macquart
  - Noud Werter
  - Darwin Rajpal
  - Mario Natella
  - Paul Lancelot
  - Tito Bordogna
  - Samuel Ijsselmuiden
- And many others



#### What are we going to discuss?

- Introduction to aeroelasticity and aeroelastic tailoring
- Modelling aspects
- Optimisation formulation
- Aeroelastically tailored results
- Experiments

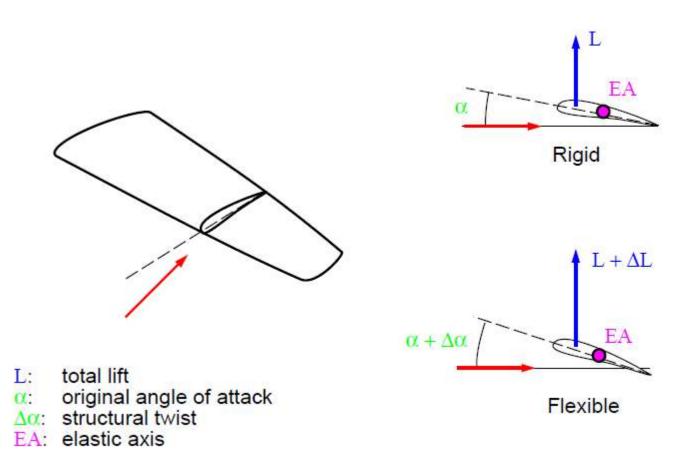


What is aeroelasticity?

Aeroelasticity deals with the behaviour of an elastic structure in an airflow where there is signification interaction between the two

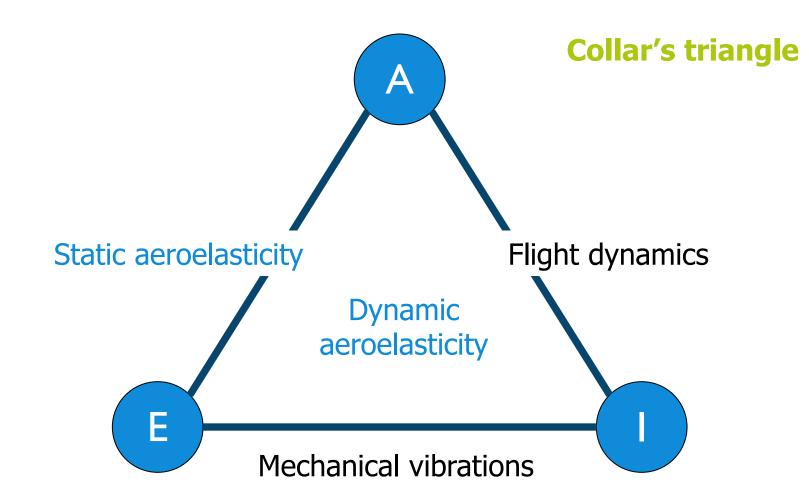


#### What is aeroelasticity?





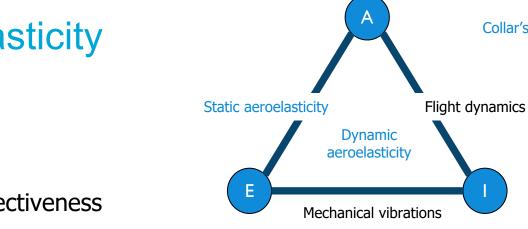
#### Aeroelastic interaction





7

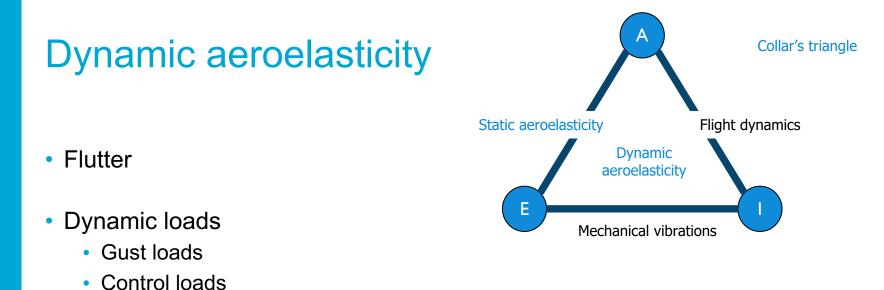
Collar's triangle



#### Static aeroelasticity

- Divergence
- Control reversal/effectiveness
- Trim
- Manoeuvre loads







#### The importance of aeroelasticity

- Calculation of jig shape of the aircraft wing
- Aircraft performance optimisation
- Aircraft weight minimisation
- Flight envelope constraining
- Ride comfort



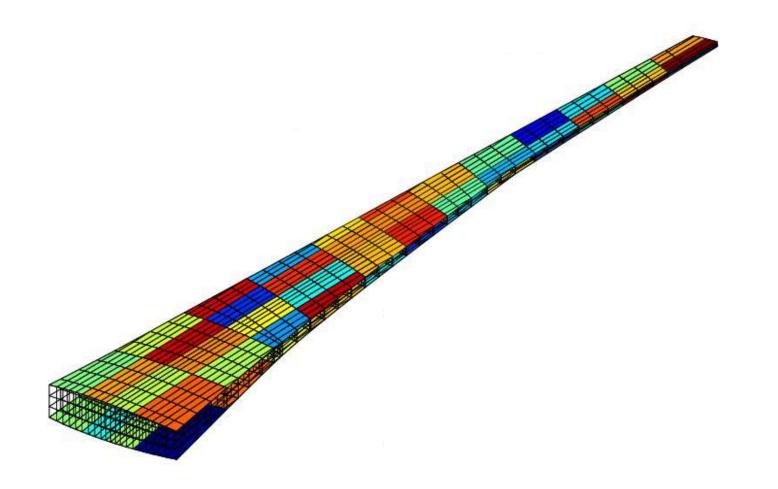
#### Aeroelastic tailoring? What is it?

The embodiment of directional stiffness into an aircraft structural design to control aeroelastic deformation, static or dynamic, in such a fashion as to affect the aerodynamic and structural performance of that aircraft in a beneficial way.

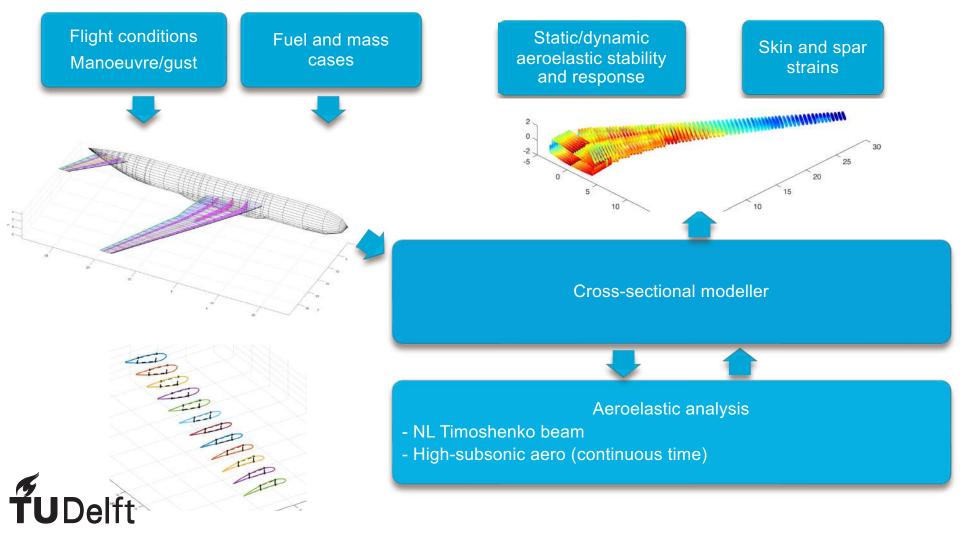
Weisshaar, 1986



#### Aeroelastic tailoring: the challenges







# PROTEUS

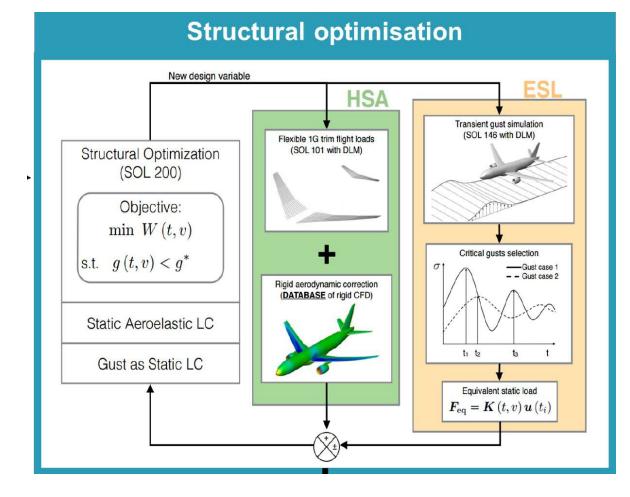
#### HiFi NASTRAN model

#### NASTRAN has limitations:

- 1. High subsonic aerodynamics only (DLM)
- 2. Limited capability to model airfoil curvature
- 3. No sensitivity analysis of dynamic loads for optimization
- 2 proposed methods to solve issues with limitations 1/2 and 3
  - 1. Hybrid static approach (HSA)
  - 2. Equivalent static loads (ESL)



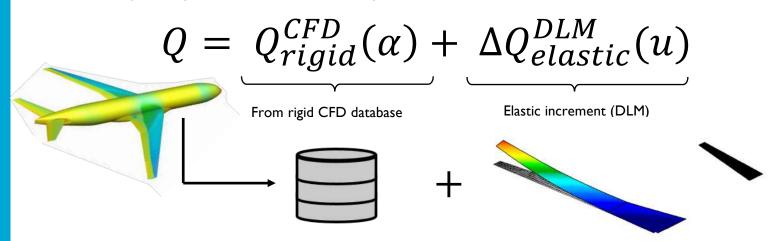
#### NASTRAN design loop





#### Correction for manoeuvres using the HSA

Developed by MSC Software, implemented in MSC NASTRAN:

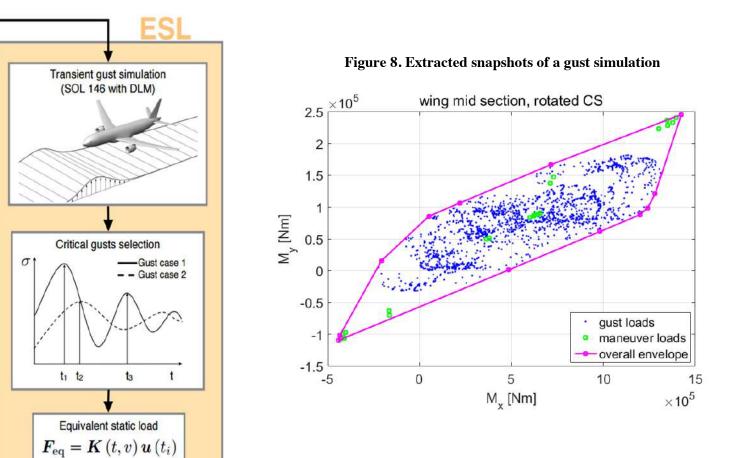


Aircraft flying at Mach 0.85, wing tip deflection approx. 5%

	Lift	Root bending	Root torsion
Coupled CFD/CSM	1.	1.	1.
Trimmed HSA	1.	1.0196	1.0093
Trimmed DLM	1.	1.1568	1.0018



#### Equivalent static load





### What will we discuss for the optimisation?

- 1. Design variables
- 2. Aeroelastic constraints
- 3. Structural constraints
- 4. Manufacturing constraints
- 5. Flight shape constraint
- 6. Objectives



#### **Design variables**



## Homogenisation

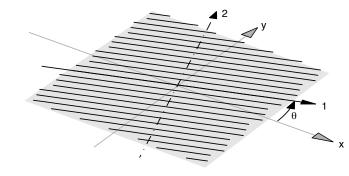
$$Q_{11} = \frac{E_1}{1 - \nu_{12}\nu_{21}},$$

$$Q_{22} = \frac{E_2}{1 - \nu_{12}\nu_{21}},$$

$$Q_{12} = \frac{\nu_{12}E_2}{1 - \nu_{12}\nu_{21}} = \frac{\nu_{21}E_1}{1 - \nu_{12}\nu_{21}},$$

$$Q_{66} = G_{12}.$$

$$\begin{cases} N_x \\ N_y \\ N_{xy} \end{cases} = \mathbf{A} \begin{cases} \varepsilon_x^0 \\ \varepsilon_y^0 \\ \gamma_{xy}^0 \end{cases} + \mathbf{B} \begin{cases} \kappa_x \\ \kappa_y \\ \kappa_{yy} \\ \kappa_{xy} \end{cases}$$
$$\begin{cases} M_x \\ M_y \\ M_{xy} \end{cases} = \mathbf{B} \begin{cases} \varepsilon_x^0 \\ \varepsilon_y^0 \\ \gamma_{xy}^0 \end{cases} + \mathbf{D} \begin{cases} \kappa_x \\ \kappa_y \\ \kappa_{yy} \\ \kappa_{xy} \end{cases}$$



$$\mathbf{A} = \sum_{k=1}^{n} \bar{\mathbf{Q}}_{(k)} (h_{k} - h_{k-1}) , \\ \mathbf{B} = \frac{1}{2} \sum_{k=1}^{n} \bar{\mathbf{Q}}_{(k)} (h_{k}^{2} - h_{k-1}^{2}) , \\ \mathbf{D} = \frac{1}{3} \sum_{k=1}^{n} \bar{\mathbf{Q}}_{(k)} (h_{k}^{3} - h_{k-1}^{3}) , \\ \mathbf{D} = \frac{1}{3} \sum_{k=1}^{n} \bar{\mathbf{Q}}_{(k)} (h_{k}^{3} - h_{k-1}^{3}) , \\ \frac{N_{x}}{N_{y}} \frac{N_{x}}{M_{x}} \frac{N_{x}}{M_{y}} \frac{N_{x}}{M_{y}} \frac{N_{x}}{M_{y}} \frac{N_{x}}{M_{y}} \frac{N_{x}}{M_{y}} \frac{N_{x}}{M_{x}} \frac{N_{x}}{M_{y}} \frac{N_{x}}{M_{x}} \frac{N_{x}}{M_{x}}$$

 $M_{xy}$ 

sym.

#### Lamination parameters

$$\begin{pmatrix} V_{1\mathbf{A}}, V_{2\mathbf{A}}, V_{3\mathbf{A}}, V_{4\mathbf{A}} \end{pmatrix} = \frac{1}{h} \int_{-h/2}^{h/2} (\cos 2\theta, \sin 2\theta, \cos 4\theta, \sin 4\theta) \, dz , \\ (V_{1\mathbf{B}}, V_{2\mathbf{B}}, V_{3\mathbf{B}}, V_{4\mathbf{B}}) = \frac{4}{h^2} \int_{-h/2}^{h/2} z (\cos 2\theta, \sin 2\theta, \cos 4\theta, \sin 4\theta) \, dz , \\ (V_{1\mathbf{D}}, V_{2\mathbf{D}}, V_{3\mathbf{D}}, V_{4\mathbf{D}}) = \frac{12}{h^3} \int_{-h/2}^{h/2} z^2 (\cos 2\theta, \sin 2\theta, \cos 4\theta, \sin 4\theta) \, dz . \\ \mathbf{A} = h(\mathbf{\Gamma}_0 + \mathbf{\Gamma}_1 V_{1\mathbf{A}} + \mathbf{\Gamma}_2 V_{2\mathbf{A}} + \mathbf{\Gamma}_3 V_{3\mathbf{A}} + \mathbf{\Gamma}_4 V_{4\mathbf{A}}) , \\ \mathbf{B} = \frac{h^2}{4} (\mathbf{\Gamma}_1 V_{1\mathbf{B}} + \mathbf{\Gamma}_2 V_{2\mathbf{B}} + \mathbf{\Gamma}_3 V_{3\mathbf{B}} + \mathbf{\Gamma}_4 V_{4\mathbf{B}}) , \\ \mathbf{D} = \frac{h^3}{12} (\mathbf{\Gamma}_0 + \mathbf{\Gamma}_1 V_{1\mathbf{D}} + \mathbf{\Gamma}_2 V_{2\mathbf{D}} + \mathbf{\Gamma}_3 V_{3\mathbf{D}} + \mathbf{\Gamma}_4 V_{4\mathbf{D}}) . \\ \begin{bmatrix} U_1 & U_4 & 0 \\ U_4 & U_1 & 0 \\ 0 & 0 & U_5 \end{bmatrix} , \quad \mathbf{\Gamma}_1 = \begin{bmatrix} U_2 & 0 & 0 \\ 0 & -U_2 & 0 \\ 0 & 0 & 0 \end{bmatrix} , \quad \mathbf{\Gamma}_2 = \begin{bmatrix} 0 & 0 & U_2/2 \\ 0 & 0 & U_2/2 \\ U_2/2 & U_2/2 & 0 \end{bmatrix} , \\ \mathbf{\Gamma}_3 = \begin{bmatrix} U_3 & -U_3 & 0 \\ -U_3 & U_3 & 0 \\ 0 & 0 & -U_3 \end{bmatrix} , \quad \mathbf{\Gamma}_4 = \begin{bmatrix} 0 & 0 & U_3 \\ 0 & 0 & -U_3 \\ U_3 & -U_3 & 0 \end{bmatrix} . \quad (1.30)$$

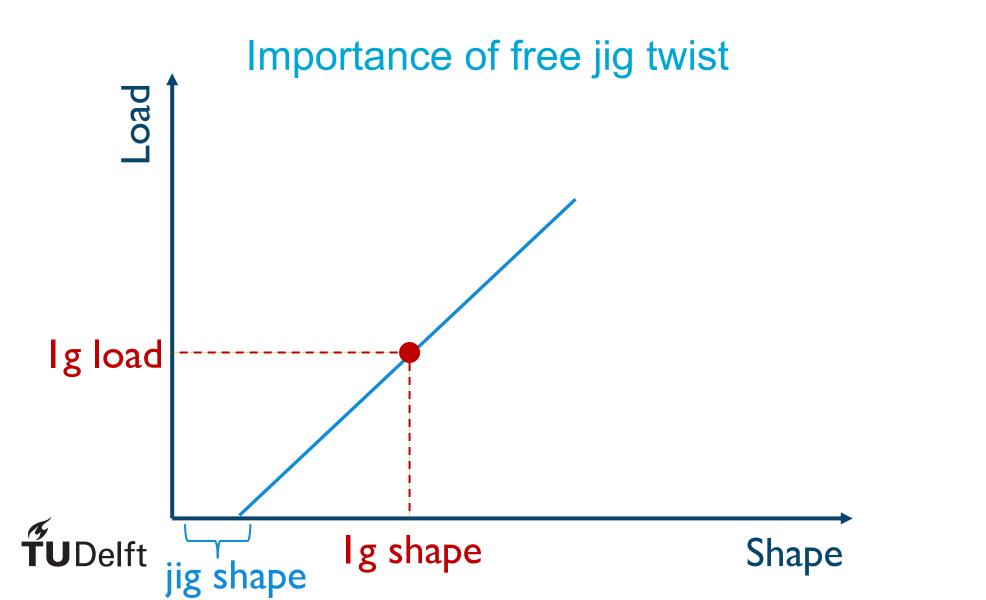
**ŤU**Delft

 $\Gamma_0 =$ 

#### Jig shape parameters

- 1g flight shape is usually determined by aerodynamics.
- Most common procedure is to reverse that 1g loads and apply them to the 1g shape to retrieve the jig shape.
- This approach does not work in case of large deflections.
- 1g shape twist is driving the aerodynamic performance, to a lesser extent also 1g shape deflection.
- Jig shape twist distribution part of the optimization, constraint on 1g twist distribution.





#### Aeroelastic constraints



#### Aeroelastic stability

• There are two types of aeroelastic stability:

- Divergence
- Flutter
- Both can be approached as an eigenvalue equation.
- Divergence is calculated automatically when carrying out a flutter analysis.



#### Aileron effectiveness

)elft

- Deflecting control surfaces and cause a nose down twist of the wing counteracting the intended roll moment.
- A minimum control effectiveness is required to keep the aircraft controllable.
- Control surface use can differ for high speed and low speed flight.

$$\begin{split} M_{\delta} + M_{p} &= 0, \\ C_{l_{\delta}}\delta(qS_{ref}s) + C_{l_{p}}p\frac{s}{V_{\infty}}(qS_{ref}s) &= 0, \\ -\frac{C_{l_{\delta}}}{C_{l_{p}}}\delta &= \frac{ps}{V_{\infty}} \end{split}$$

## Class of Aircraft

## Level of Maneuvera bility

Category of Maneuver



## Class of Aircraft

- Class I Ultralight aircraft.
- Class II Assault, bomber etc.
- Class III *Commercial etc.*

## Level of Maneuvera bility

Category of Maneuver



## Class of Aircraft



Level of Maneuvera bility

Adequate.

• L2 Acceptable.

• L3 *Controllable.*  Category of Maneuver

## Class of Aircraft

Level of Maneuvera bility Category of Maneuver

A *Combat.*B *Gradual maneuvers.*C *Taka-off landing*



## Class of Aircraft

- Class I Ultralight aircraft.
   Class II Assault homber et
- Class III *Commercial etc.*

## Level of Maneuvera bility

- L1 *Adequate.*
- L2 Acceptable.
- L3 *Controllable.*

## Category of Maneuver

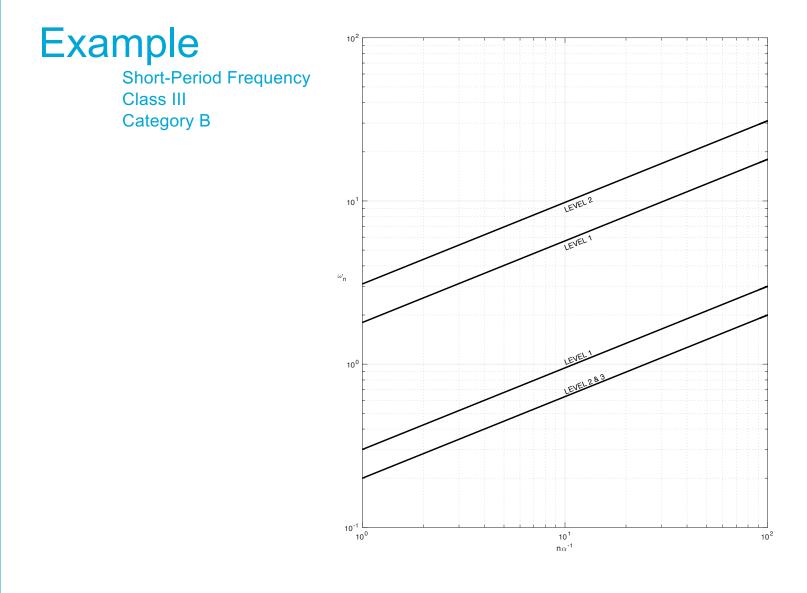
Combat. B Gradual maneuvers.



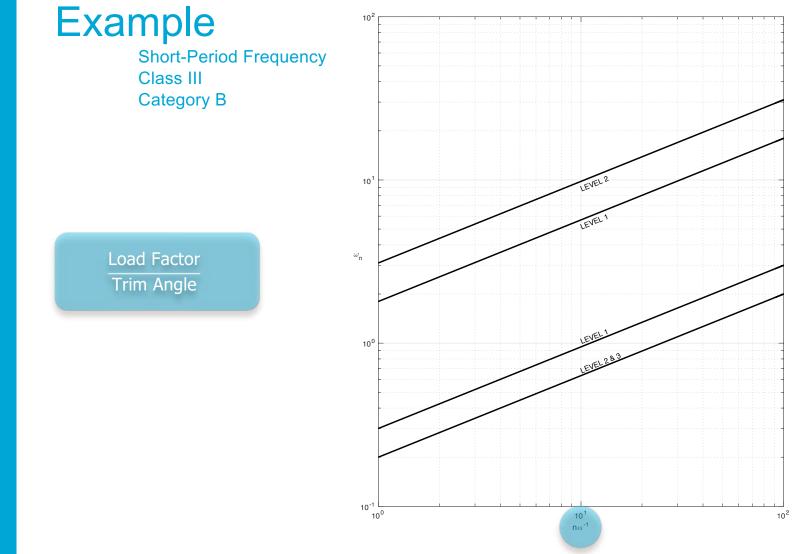
#### Handling Qualities MIL-HDBK-1797 3.2 Longitudinal Flight Qualities

- Short-Period Frequency and Damping
- Phugoid Damping
- Flight Path Angle

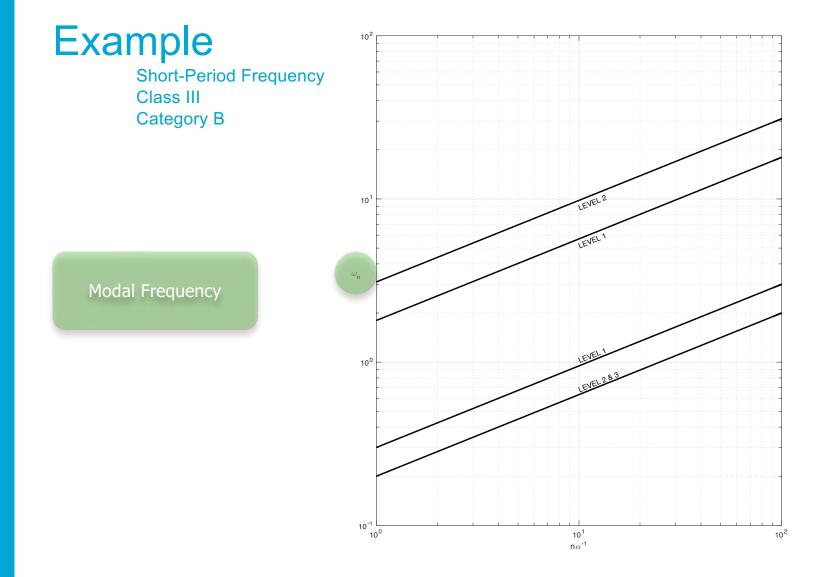
**U**Delft



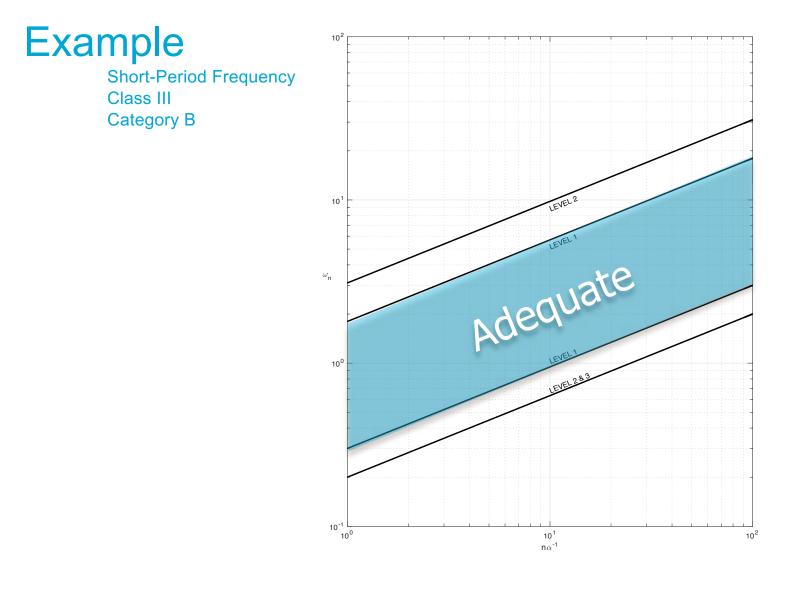




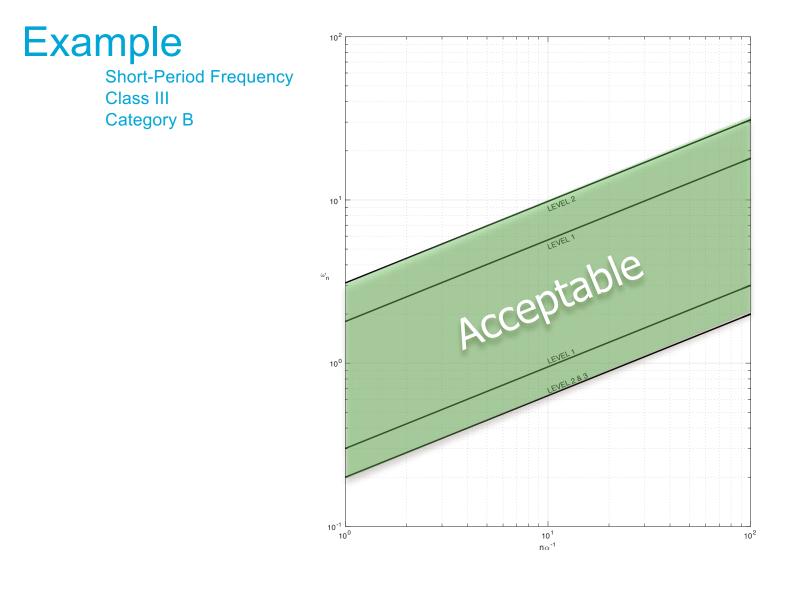
**TU**Delft



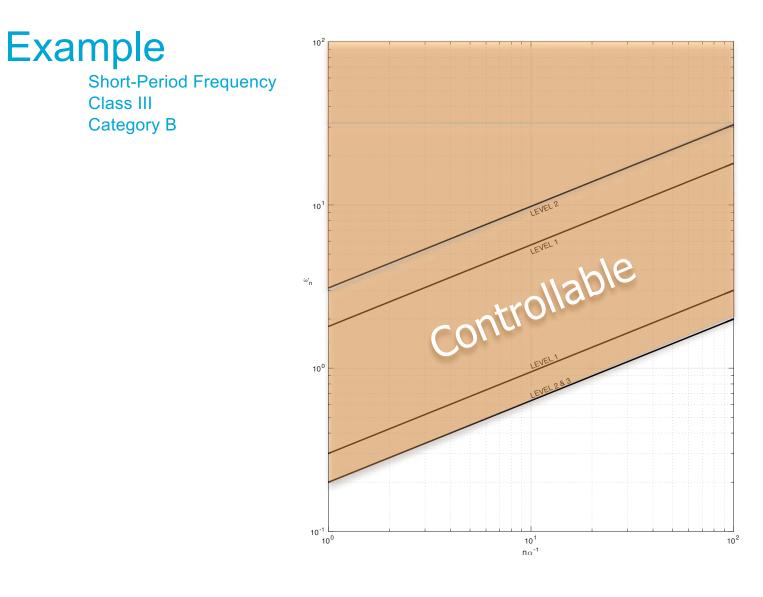














### Structural constraints



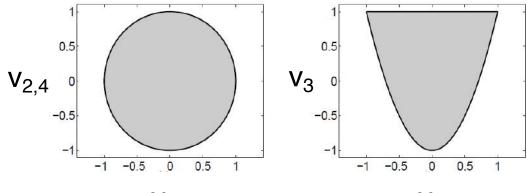
### Laminate feasibility

- There must be a feasible combination between lamination parameters to retrieve feasible stacking sequence.
- In-plane and out-of-plane lamination parameters can not be chosen independently.

$$2V_1^2 (1 - V_3) + 2V_2^2 (1 + V_3) + V_3^2 + V_4^2 - 4V_1V_2V_4 \le 1$$
$$V_1^2 + V_2^2 \le 1$$
$$-1 \le V_i \le 1$$

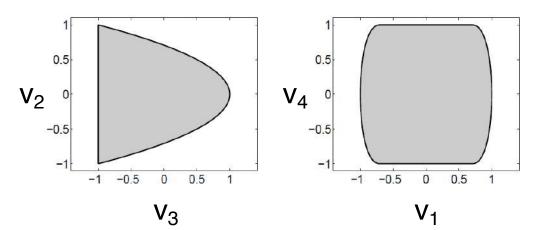


## Laminate feasibility











# **Buckling**

- Only inter-rib and inter-stiffener buckling is considered.
- The buckling panels are assumed to be simply supported.
- Panels transformed to a domain ranging from -1 to 1 using a bilinear transformation.
- The load is assumed to be constant over a panel in a certain direction.



#### Failure

• Tsai-Wu first ply failure criterion.

$$F_{11}\sigma_1^2 + F_{22}\sigma_2^2 + F_{66}\tau_{12}^2 + F_1\sigma_1 + F_2\sigma_2 + 2F_{12}\sigma_1\sigma_2 = 1$$
  
$$F_{11} = \frac{1}{XX} \qquad F_{22} = \frac{1}{XX} \qquad F_1 = \frac{1}{X} - \frac{1}{X}$$

$$F_{2} = \frac{1}{Y_{t}} - \frac{1}{Y_{c}} \qquad F_{12} = \frac{-1}{2\sqrt{X_{t}X_{c}Y_{t}Y_{c}}} \qquad F_{66} = \frac{1}{S^{2}}$$

• Related to strain measures through the Q matrix:

$$G_{11}\epsilon_1^2 + G_{22}\epsilon_2^2 + G_{66}\epsilon_{12}^2 + G_1\epsilon_1 + G_2\epsilon_2 + 2G_{12}\epsilon_1\epsilon_2 = 1$$

Transformation from material strains to laminate strains

$$\begin{bmatrix} \frac{1}{2}(1+c) & \frac{1}{2}(1-c) & s \\ \frac{1}{2}(1-c) & \frac{1}{2}(1+c) & -s \\ -\frac{1}{2}s & \frac{1}{2}s & c \end{bmatrix}$$



SKhani, A., IJsselmuiden, S.T., Abdalla, M. M., & Gürdal, Z. (2011). Design of variable Composites maximum strength using lamination parameters. 42(3), 546-552 stiffness panels for Part B: Engineering,

#### Failure

• Failure is governed by this equation:

$$F(\epsilon_x, \epsilon_y, \epsilon_{xy}, s, c) = 0$$

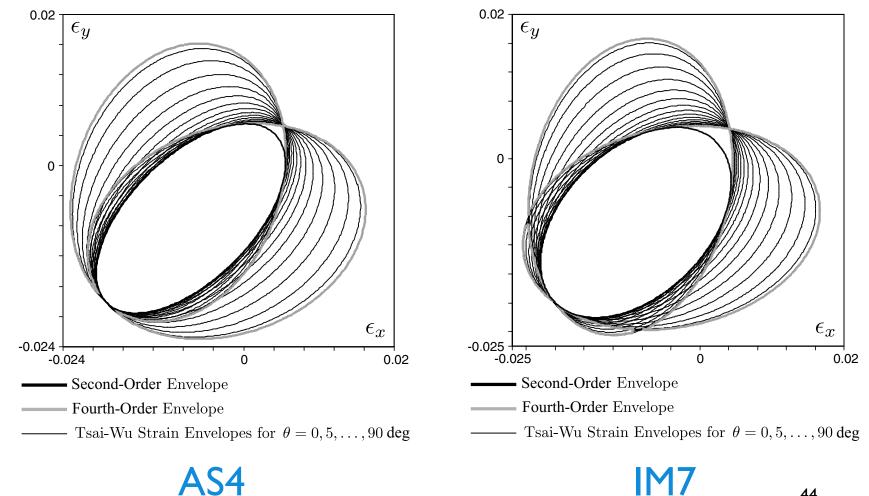
 Needs to be written for lamination parameters, i.e. independent of the ply angles: eliminate the ply angle by imposing two additional equations

• The trigonometric relation  $\cos^2 \theta + \sin^2 \theta = 1$ 

• A surface tangential to all failure functions for each  $\theta$ ,  $\frac{dF}{d\theta} = 0$ 

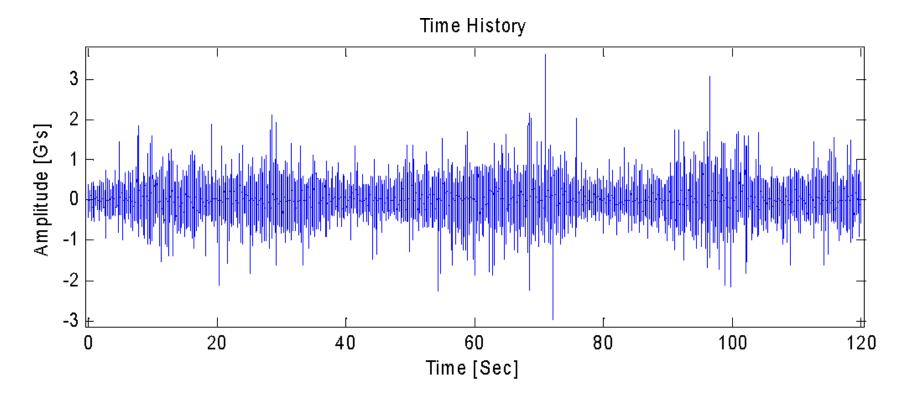


#### Failure envelope examples





## Effect of fatigue loads

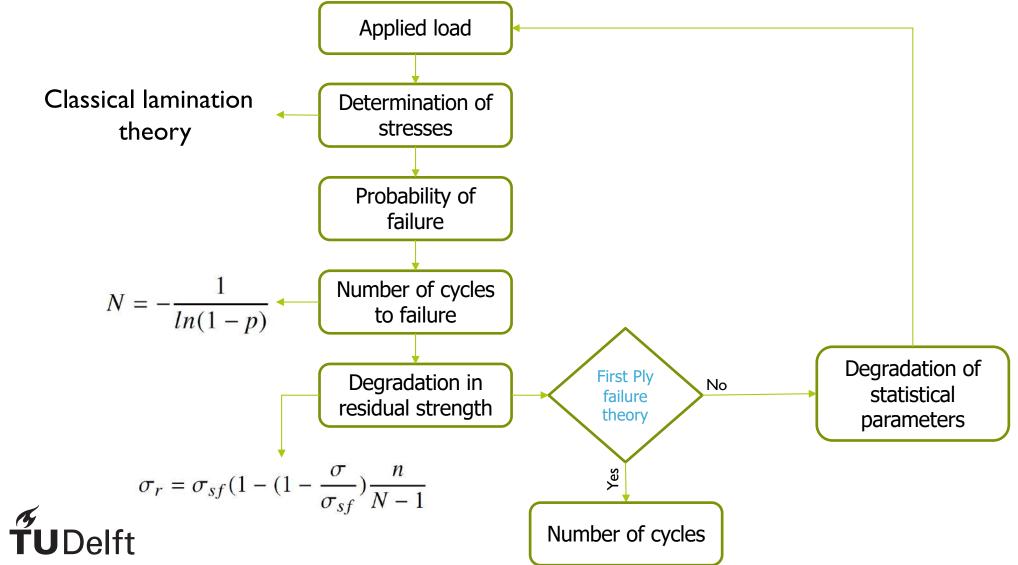




## Design for number of flight cycles

- **Standard practice**: apply knock-down factor to material allowables to ensure a no-fatigue design.
- **Proposed solution**: design the lifting surface to fail at a prescribed amount of flights.
- Methodology: combine probability of failure at a certain number of cycles with Tsai-Wu failure theorem.





## Applied loads are obtained from TWIST

Flight type	Number of flights in one block of 4000 flights	I 1.60	II	umber a III 1.30	IV 1.15	v 0.995	VI 0.84	f ampli VII 0.685 er fligi	VIII 0.53	rel IX X 0.375 0.222		22	Total number of cycles per flight		
A	1	1	1	1	4	8	18	64	112	391	(391)	900	(0)	1500	(600)
в	1	-	1	1	2	5	11	39	76	366	(385)	899	(0)	1400	(520)
с	3			1	1	2	7	22	61	277	(286)	879	(0)	1250	(380)
D	9				1	1	2	14	44	208	(208)	680	(0)	950	(270)
Е	24	,				1	1	6	24	165	(168)	603	(0)	800	(200)
F	60	-					1	. 3	19	115	(107)	512	(0)	650	(130)
G	181							1	7	70	(72)	412	(0)	490	(80)
н	420								1	16	(16)	233	(23)	250	(40)
I	1,090									1	(1)	69	(4)	70	(5)
Ј	2,211											25	(2)	25	(2)
Total number of cycles per block of 4000 flights		1.	2	5	18	52	152	800	4170	3480 (348		358665 (18442)			
Cumulative number of load cycles per block of 4000 fl.		1	3	8	26	78	230	1030	5200	4000	00	398665 (58442)			



Lowak, H., DeJonge, J., Franz, J., and Schütz, D., "MINITWIST - A shortened version of TWIST," NLR MP79018U, 1979.



# Manufacturing constraints

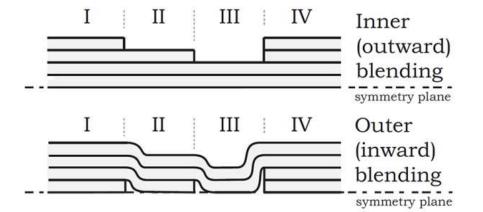


# NASA rules for composite manufacturing

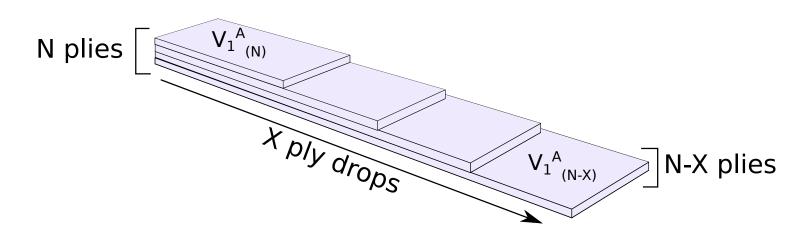
- Symmetric laminates: This rule is generally applied to avoid out of plane deformation during the curing process, due to the in-plane extension of the laminate.
- Balanced laminates: same number of plies with orientation equal to  $\theta$  and  $-\theta$  so that  $A_{16}=A_{26}=0$ .
- Contiguity rule: no more than 4 successive plies with the same orientation.
- Blending rule: ply continuity need to be ensured from one panel to another.
- Restricted angle: a limited set of ply orientation is available to build the laminate. Known as the classical orientation, they are equivalent to [0/90/±45].
- Disorientation rule: no more than  $\pm 45$  difference between successive layers in order to avoid inter-plies stresses.
- Percentage rule: a minimum of 10% of the plies must be in each of the following direction: 0, 45, 90 and -45. This should ensure that the structure is robust enough to carry secondary loading.



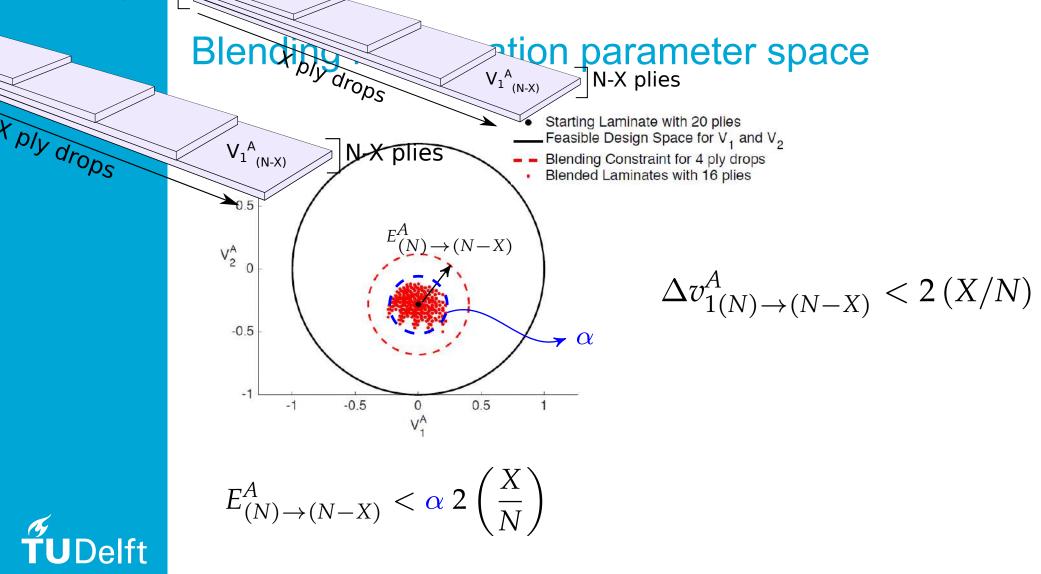
### **Blending constraints**



- Inner vs outer blending.
- Blending can be defined:
  - During stacking sequence retrieval.
  - During continuous optimization.







### Flight shape constraint



# 1g shape constraint

- 1g shape or flight shape or cruise shape is given by the aerodynamics department.
- Often multiple points are defined during a cruise phase.
- Cruise shape depends on stiffness distribution of the wing and the jig shape.
- Jig shape optimization can be approached in two ways:
  - Classical: take 1g loads and 1g shape and retrieve jig shape by inverting 1g loads.
  - Advanced: include jig twist as design variables.



## **Objectives**



## **Objectives**

• Structural mass minimization  $\rightarrow$  payload increase.

• Range  

$$R = \frac{V}{g \cdot SFC} \frac{C_L}{C_D} ln\left(\frac{W_i}{W_f}\right)$$

• Material coupling is not a goal in itself.

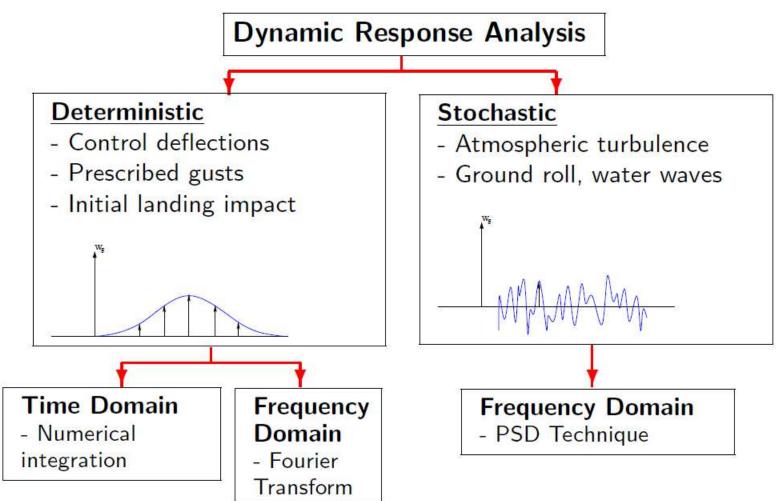


# Types of loads

- Flight loads
  - Manoeuvre/static loads
  - Dynamic loads
- Ground loads

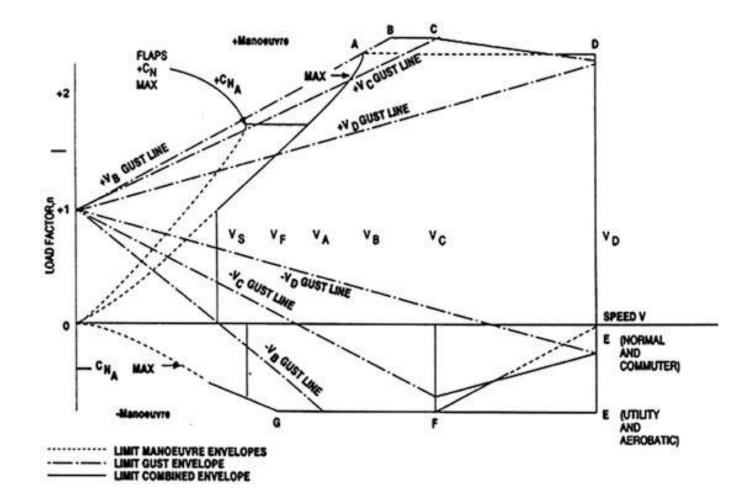


## **Dynamic loads**





## V-n diagram

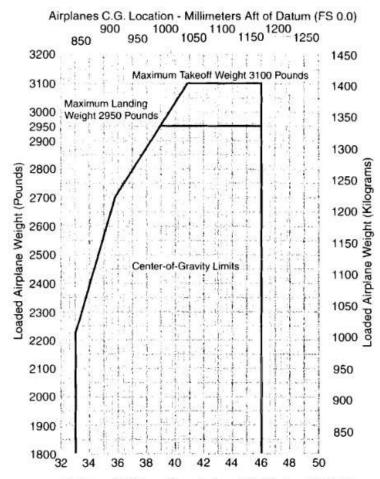




CESSNA SECTION 6 MODEL 182T NAV III WEIGHT AND BALANCE/EQUIPMENT LIST

**CENTER-OF-GRAVITY LIMITS** 

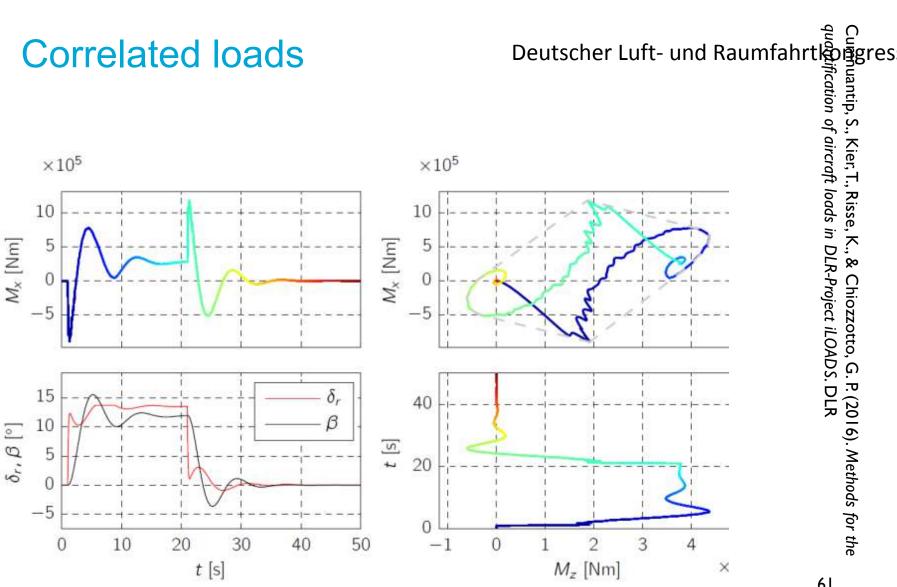
64,570



**TU**Delft

Airplanes C.G. Location - Inches Aft of Datum (FS 0.0)





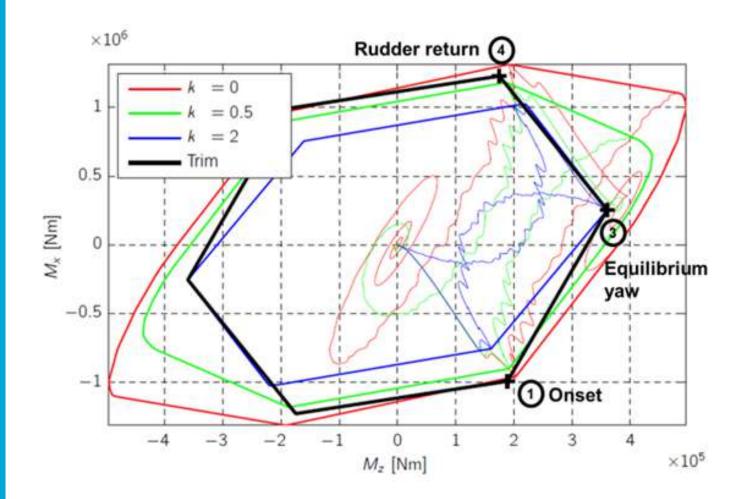
#### **Correlated loads**

61

Chiozzotto, G. P. (2016). Methods for the

### Load envelopes

**TU**Delft



quantification of aircraft loads in DLR-Project iLOADS. DLR Cumnuantip, S., Kier, T., Risse, K., & Chiozzotto, G. P. (2016). Methods for the

# Typical number of load cases

Flight Points	50
Mass Cases	100
Control Surface Configuration	10
Manoeuvres and Gusts	50
Control Laws	4
Total Number of Cases	10,000,000



#### Load case selection

- A significant amount of load cases need to be considered to size the wing structure.
- The entire loads process is too time consuming.
- Only a few load cases are sizing.
- The sizing load cases could change during the design process.



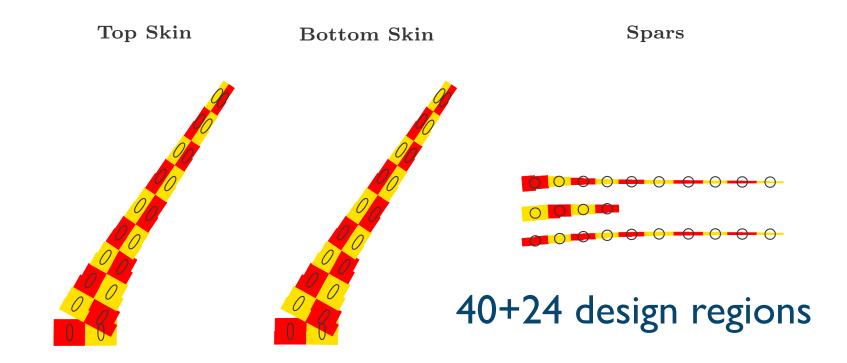
### Aeroelastically tailored results

- Typical tailored wing results
- Effect of aileron effectiveness
- Effect of 1g shape constraint and free jig shape
- Effect of MLA
- Effect of fatigue constraints
- Effect of blending
- Criticality of gust loads



#### **Design regions**

UD carbon/epoxy (AS4/3501-6)





- I. Predefined laminates
- 2. Unbalanced laminates

### Visualisation of the laminate stiffness

$$E_{m_{11}}(\theta) = \frac{1}{A_{11}^{-1}(\theta)}$$
$$E_{f_{11}}(\theta) = \frac{1}{D_{11}^{-1}(\theta)}$$

$$A_{11}^{-1}(\theta) = T^T A_{11}^{-1} T$$
$$D_{11}^{-1}(\theta) = T^T D_{11}^{-1} T$$

$$T = \begin{bmatrix} \cos^2(\theta) & \sin^2(\theta) & 2\cos(\theta)\sin(\theta) \\ \sin^2(\theta) & \cos^2(\theta) & -2\cos(\theta)\sin(\theta) \\ -\cos(\theta)\sin(\theta) & \cos(\theta)\sin(\theta) & \cos^2(\theta) - \sin^2(\theta) \end{bmatrix}$$

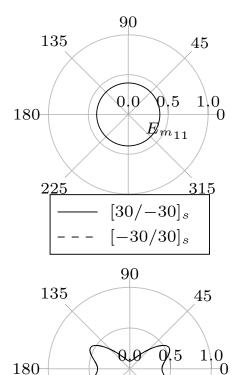


#### Examples of the visualisation

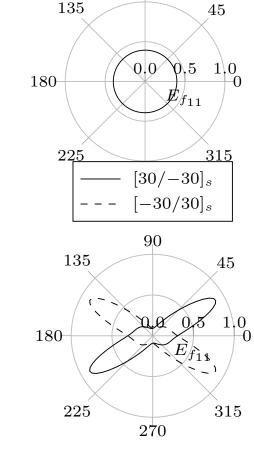
 $E_{n_{11}}$ 

270

315



225



90

Quasiisotropic

Symmetric balanced



## **Optimisation responses**

**TU**Delft

	Туре	# responses			
Objective	Mass	1			
	Lamination parameters	512			
Design variables	Laminate thickness	64			
	Jig twist	20			
	Lamination parameters feasibility	384			
	1g twist	20			
	Aeroelastic stability	10 per LC			
Constraints	Local AoA	34 per LC			
	Aileron effectiveness	1 per LC			
	Tsai-Wu failure criterion	1024 per LC			
	Buckling factor	4096 per LC			
	Total	1001 + 5156 per LC			



ID	Description	EAS [m/s]	Altitude [m]	Mach [-]	n <sub>z</sub> [-]	Fuel		
1	Cruise	136	11,000	0.85	1.0	70%		
2	Pull up	240	3,000	0.85	2.5	80%		
3	Push down	198	0	0.60	-1.0	80%		
4	Dynamic	156	0	0.46	1.0	80%		
	Gust length [m]	50, 60, 70, 80, 90, 100, 107						

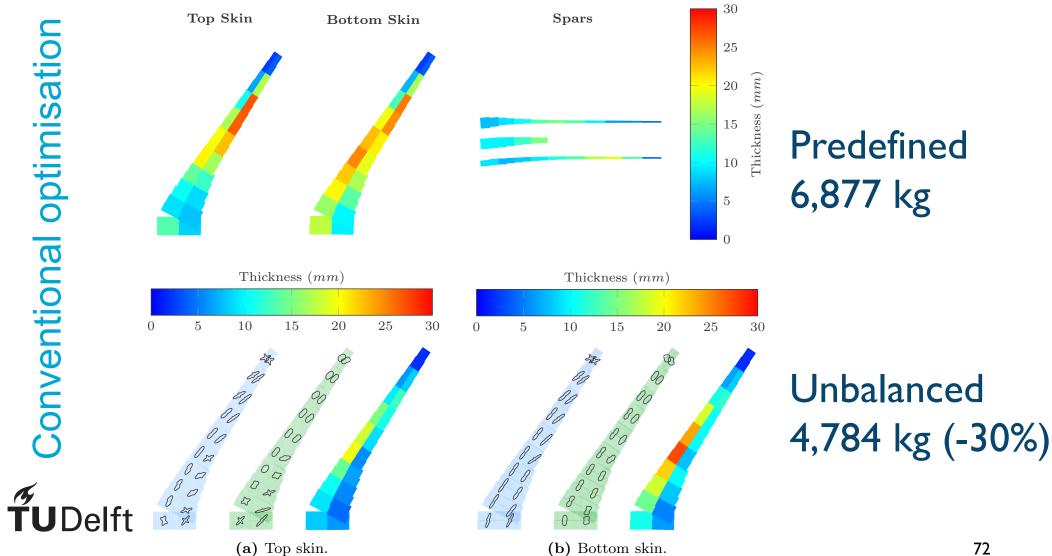


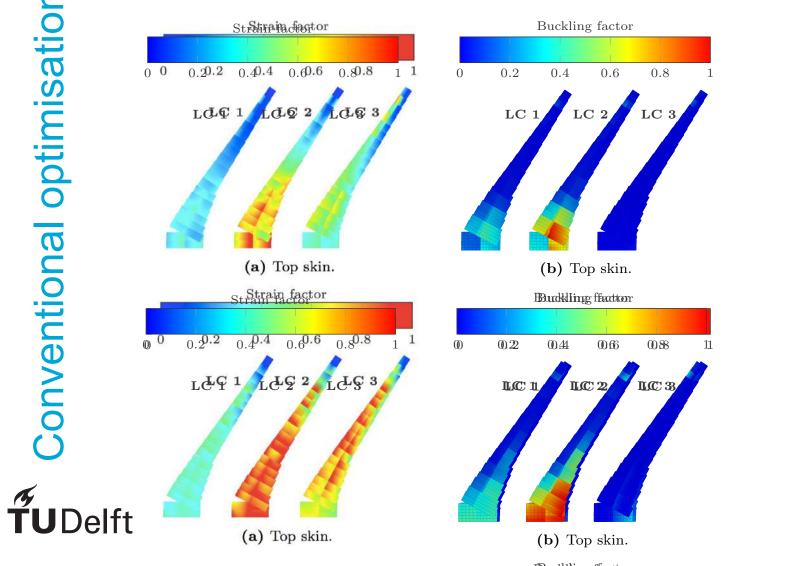
Static design:3 LCDynamic design:10+ LC (multiple points in time history)

## Aeroelastically tailored results

- Typical tailored wing results
- Effect of aileron effectiveness
- Effect of 1g shape constraint and free jig shape
- Effect of MLA
- Effect of fatigue constraints
- Effect of blending
- Criticality of gust loads







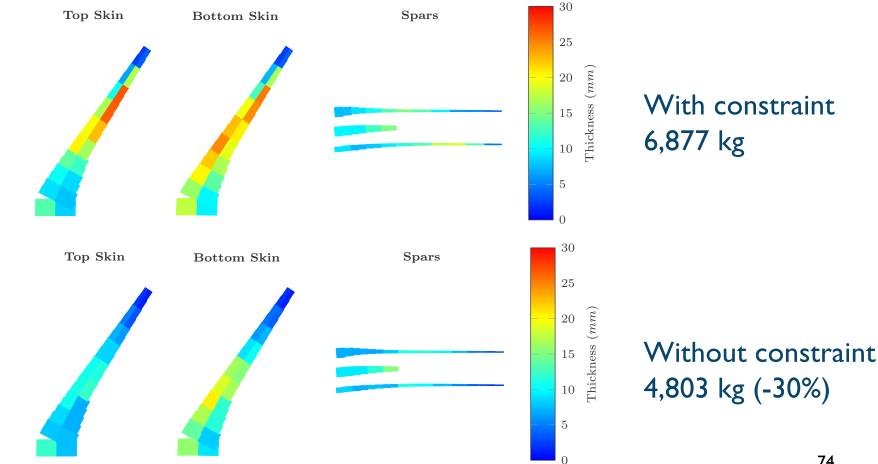
# Predefined

#### Unbalanced

#### **Predefined** laminates

#### **Conventional optimisation** Effect of control effectiveness

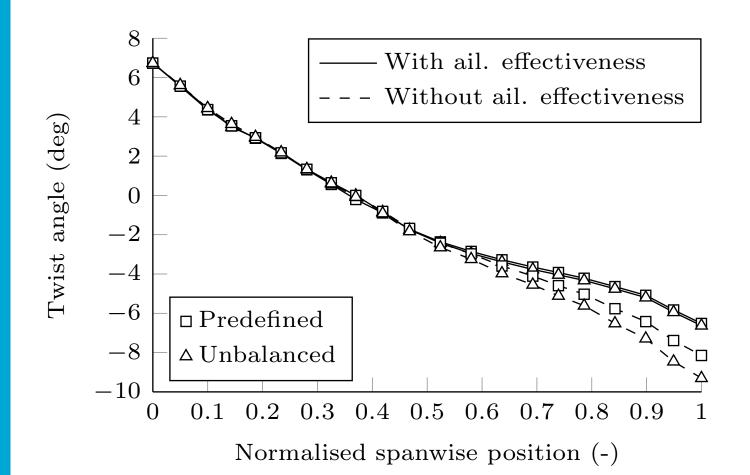
**J**Delft



- Typical tailored wing results
- Effect of aileron effectiveness
- Effect of 1g shape constraint and free jig shape
- Effect of MLA
- Effect of fatigue constraints
- Effect of blending
- Criticality of gust loads



#### 2.5g twist

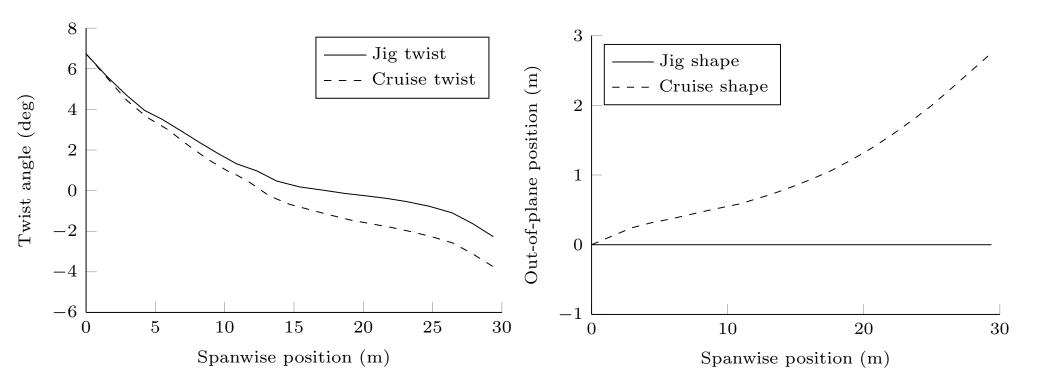




- Typical tailored wing results
- Effect of aileron effectiveness
- Effect of 1g shape constraint and free jig shape
- Effect of MLA
- Effect of fatigue constraints
- Effect of blending
- Criticality of gust loads



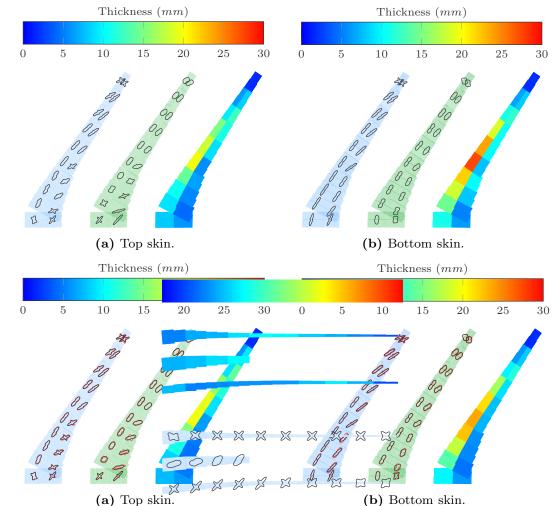
#### Predefined jig shape



**TU**Delft

#### Unbalanced laminates

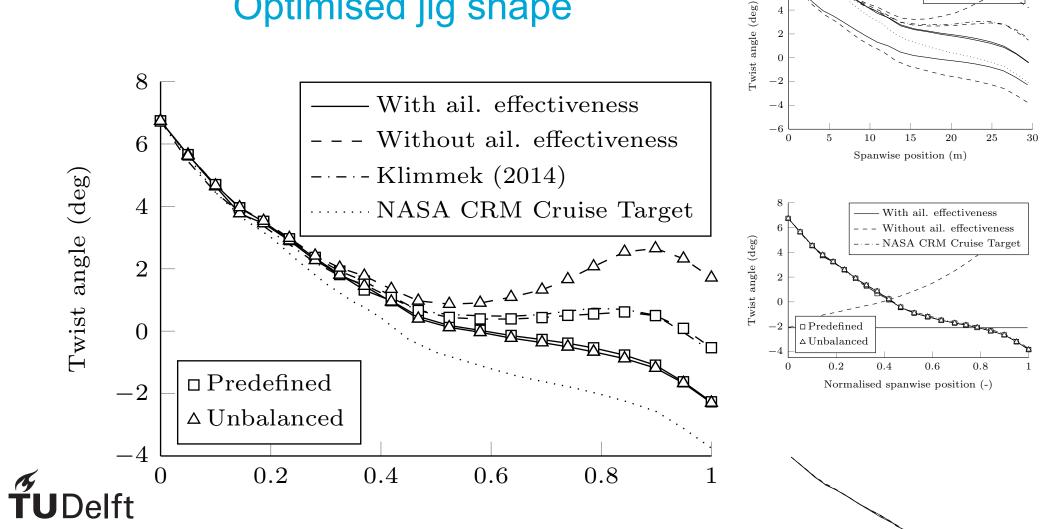
### Including free jig twist



# Fixed jig twist 4,784 kg

## Free jig twist 4,517 kg (-6%)

### **Optimised jig shape**



8

6

 $\mathbf{2}$ 

80

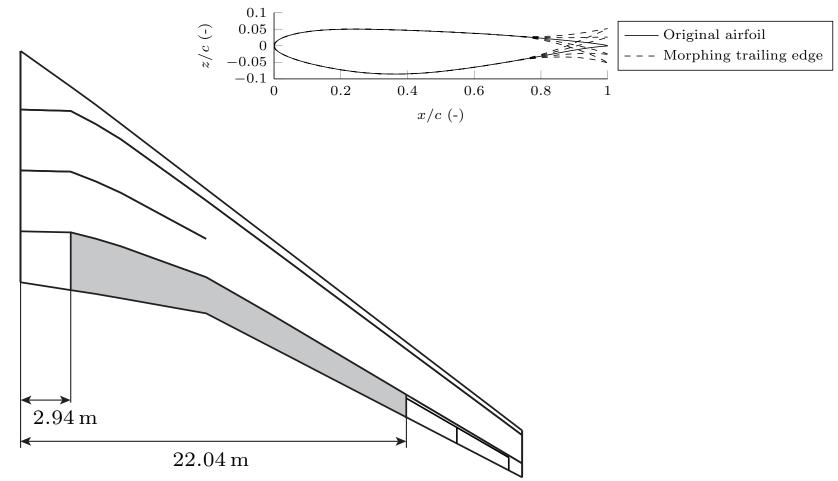
Jig twist

Cruise twist

- Typical tailored wing results
- Effect of aileron effectiveness
- Effect of 1g shape constraint and free jig shape
- Effect of MLA
- Effect of fatigue constraints
- Effect of blending
- Criticality of gust loads

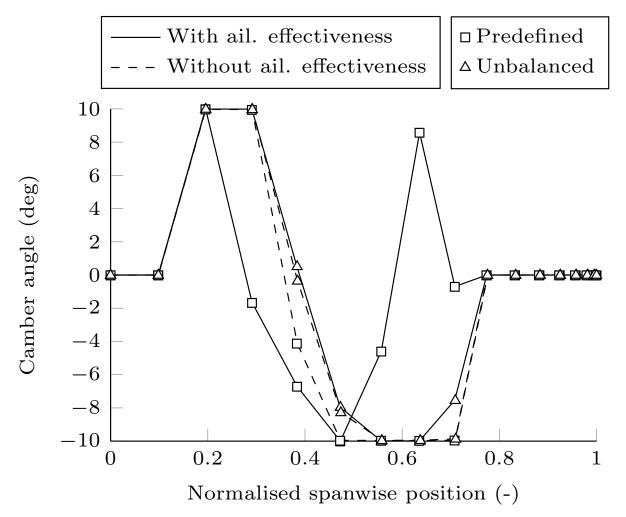


#### Active control surfaces





#### Control deflections under 2.5g load

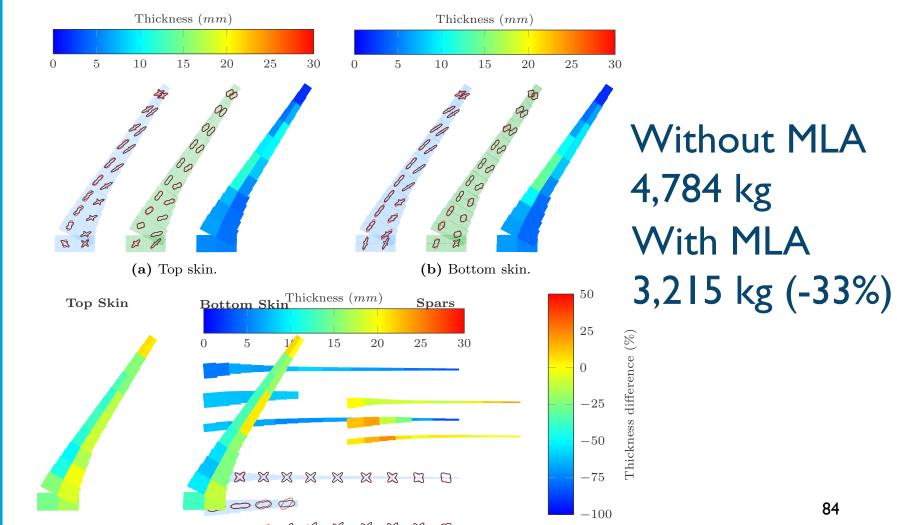




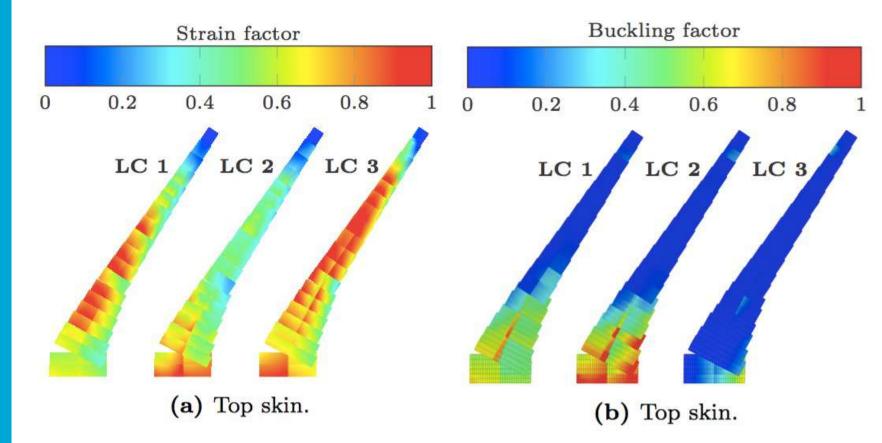
#### Unbalanced laminates

#### **Thickness distribution**

**TU**Delft



### Strain and buckling

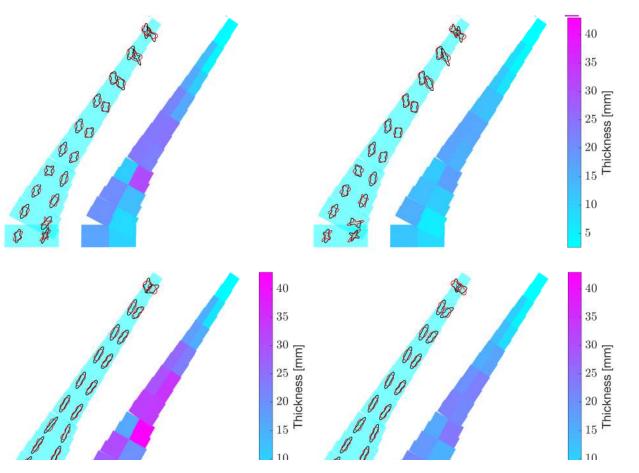




- Typical tailored wing results
- Effect of aileron effectiveness
- Effect of 1g shape constraint and free jig shape
- Effect of MLA
- Effect of fatigue constraints
- Effect of blending
- Criticality of gust loads

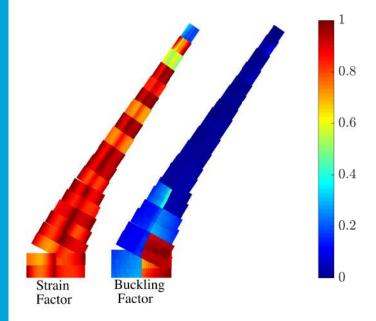


#### Skin thickness results

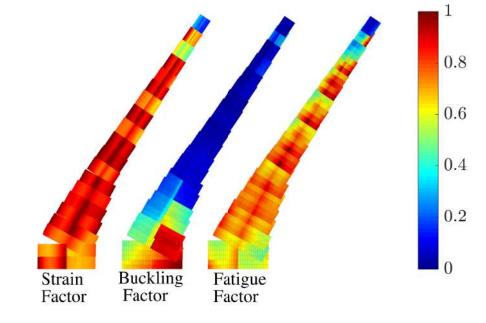




#### Constraint values top skin

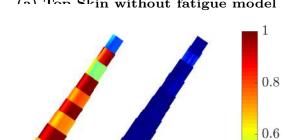


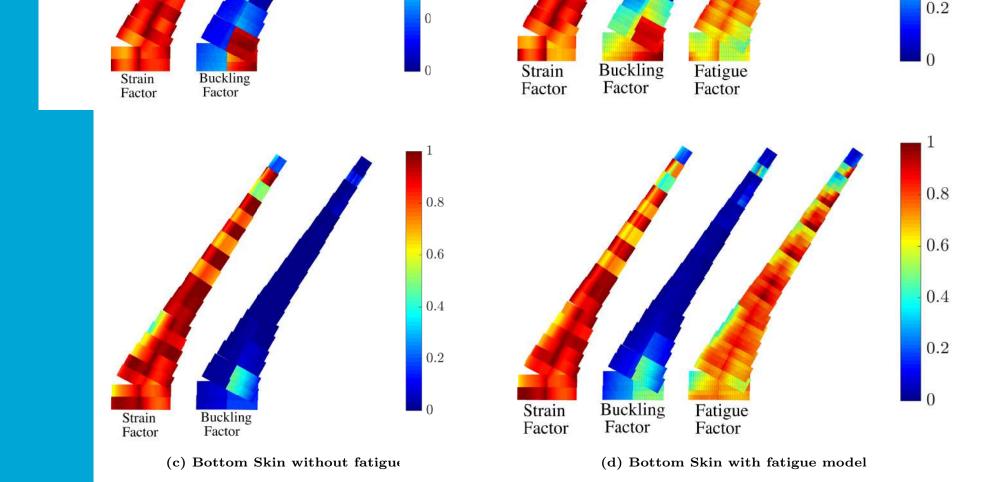
(a) Top Skin without fatigue model











Ť

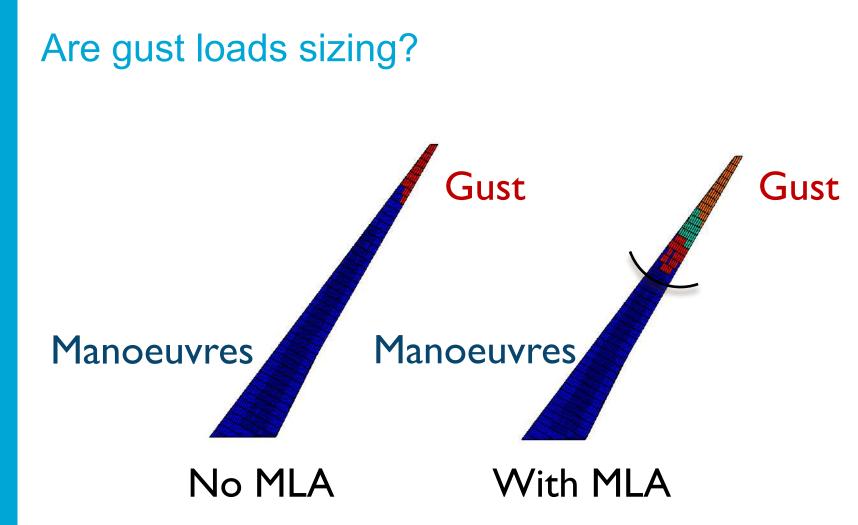
#### Mass comparison

Туре	Tailored	Units
With fatigue model	9,416	kg
Without fatigue model	12,129	kg
Difference (%)	22	%



- Typical tailored wing results
- Effect of aileron effectiveness
- Effect of 1g shape constraint and free jig shape
- Effect of MLA
- Effect of fatigue constraints
- Effect of blending
- Criticality of gust loads

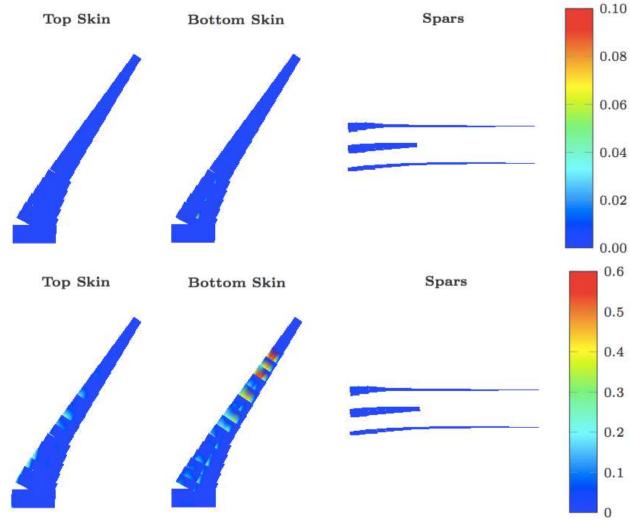






**Gust loads critical?** 

**TU**Delft

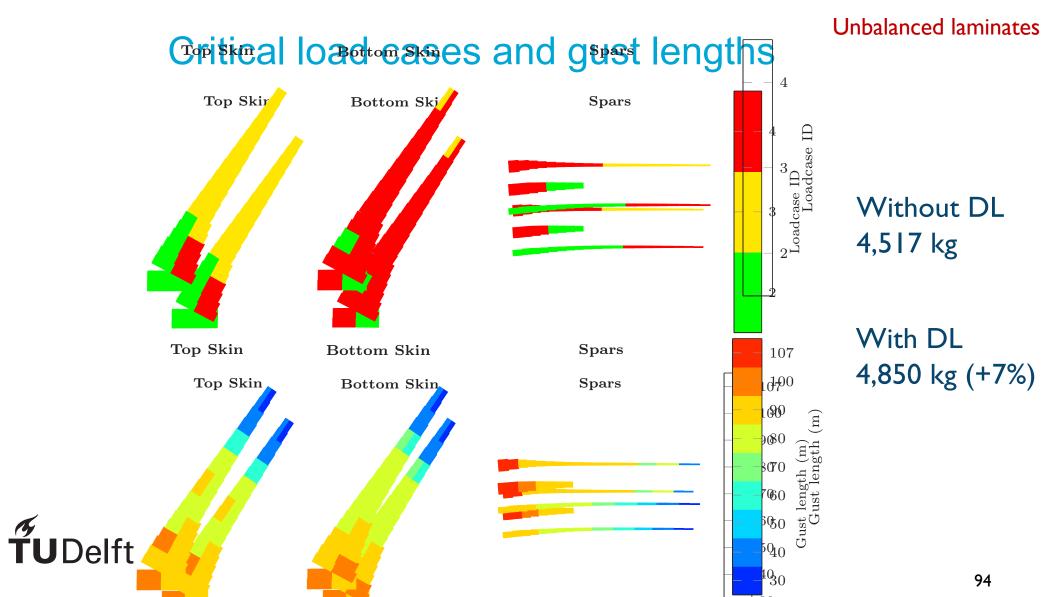


Predefined

Strain factor violation

Strain factor violation





#### What's next in aeroelastic tailoring

- More focus on high fidelity methods.
- Include control into the design.
- Coupling to other disciplines (MDAO).
- More advanced measuring techniques, also in flight.
- Scaled flight testing.
- Industrialisation of the technology link to advanced manufacturing.
- Novel (composite) materials.

